

# Quantum computing in the noise environment: variational approach and error correction

Aleksey Fedorov **Russian Quantum Center** 

Theory: E. Kiktenko (RQC), I. Luchnikov (RQC), M. Sapova (RQC), A. Boev (RQC), A. Antipov (RQC) et. al.

LRC collaboration

Industry collaboration: Nissan (Japan), Gero AI (Singpore), Genotek (Russia)







#### 40 years of quantum computing



#### Yury Manin, Computable and non-computable (1980)

Editorial Published: 10 January 2022

#### 40 years of quantum computing

Nature Reviews Physics4, 1 (2022)Cite this article3388Accesses21AltmetricMetrics

This year we celebrate four decades of quantum computing by looking back at the milestones of the field and forward to the challenges and opportunities that lie ahead.



#### Richard Feynman, Simulating physics with computers (1981)

#### Quantum computing 40 years later

#### John Preskill

Forty years ago, Richard Feynman proposed harnessing quantum physics to build a more powerful kind of computer. Realizing Feynman's vision is one of the grand challenges facing 21st century science and technology. In this article, we'll recall Feynman's contribution that launched the quest for a quantum computer, and assess where the field stands 40 years later.

Comments:	49 pages. To appear in Feynman Lectures on Computation, 2nd edition, published by Taylor & Francis			
	Group, edited by Anthony J. G. Hey. (v2) typos corrected			
Subjects:	Quantum Physics (quant-ph)			
Cite as:	arXiv:2106.10522 [quant-ph]			
	(or arXiv:2106.10522v2 [quant-ph] for this version)			

# 40 years of quantum computing: Main challenges

for the quantum computing technology?





- devices efficiently?
- of quantum computing?

How to factor 2048 bit RSA integers in 8 hours using 20 million noisy qubits

known approach. By laying out and optimizing the surface-code resources required of our approach we show that FeMoCo can be simulated using about four million physical qubits and under 4 days of runtime, assuming 1- $\mu$ s cycle times and physical gate-error rates no worse than 0.1%.

Craig Gidney, Martin Ekerå

C. Gidney and M. Ekerå, How to factor 2048 bit RSA integers in 8 hours using 20 million noisy qubits, arXiv:1905.09749; J. Lee, Even more efficient quantum computations of chemistry through tensor hypercontraction, arXiv:2011.03494.

Physical platform for quantum computing: What can be an analog of a 'silicon transistor'



Efficient error correction: Is it possible to develop efficient error correction techniques and enter the era of fault-tolerant quantum computing? Is it possible to use existing NISQ

#### Quantum algorithms and applications: What are most interesting near-term applications



# Origin of a quantum speedup

- all possible solutions in parallel.
- •
- •

<u>Classical system</u>

A single bit string of n zeros and ones

Gottesman-Knill theorem: Even some highly entangled states can be simulated efficiently. •

• "Naive quantum parallelism" (D. Deutsch): Quantum computers solve problems by trying

Access to exponentially large computational spaces: However, such an "access" takes place also for classical systems since N classical bits can take 2<sup>N</sup> possible values.

Quantum complexity (J. Preskill): Quantum information is very different in that writing down a complete description of just one typical configuration of N qubits is complex.

Quantum system

2<sup>n</sup> complex numbers

# Origin of a quantum speedup in the NISQ era

- a noisy channel.
- Quantum advantage experiments: Is it possible to demonstrate (useful) quantum advantage in the presence of noise?



Q. Zhu et al., Quantum Computational Advantage via 60-Qubit 24-Cycle Random Circuit Sampling, https://arxiv.org/abs/2109.03494

Role of decoherence: The control of decoherence of a qubit is a central problem of various models of quantum computation, where an incoming qubit is transmitted through

# Quantum computing applications

mainly, physics and computer science.

#### Quantum phases of matter on a 256-atom programmable quantum simulator

How to factor 2048 bit RSA integers in 8 hours using 20 million noisy qubits

Craig Gidney<sup>1</sup> and Martin Ekerå<sup>2</sup>

optimization, and machine learning

Scientific applications: Use quantum computers to explore new frontiers in science,

#### Scaling advantage over path-integral Monte Carlo in quantum simulation of geometrically frustrated magnets

Specialized applications: random number generation, cryptoanalysis, sampling (?).

**Post-Quantum Cryptography** PQC



(Potentially) widespread applications: simulation (quantum and quantum-enhanced),

# Quantum computing applications

#### **Simulation**



#### Quantum:

- Chemistry
- Biophysics
- Materials
- Drugs
- . . .

#### Classical:

- Linear equations
- Differential equations





- •
- •
- . . .

### **Optimization**

Logistics Finance Job scheduling

#### Machine learning



- Training networks
- Speed-up linear algebra
- Quantum kernel • models

# Quantum computing applications: Simulation (chemistry) & Optimization

#### IONQ: Optimizing electronic structure simulations on a trapped-ion quantum computer using problem decomposition

14 Feb 2021

Simulating a ring of 10 hydrogen atoms without freezing any electrons

https://www.nature.com/articles/s42005-021-00751-9.pdf

#### **QBoard & Nissan with IBM: Variational** quantum eigensolver techniques for simulating carbon monoxide oxidation

Simulating a set of molecules, O2, CO, and CO2, participating in the carbon monoxide oxidation processes.







#### 25 Aug 2021

#### Delta Airlines: Exploring Airline Gate-Scheduling Optimization Using Quantum Computers

#### 18 Nov 2021

One of the many complex problems facing the airline industry today is how to optimize large combinations of cargo and passenger traffic among the planes, gates, personnel and the air traffic flows originating or terminating at an airport

https://arxiv.org/abs/2111.09472



# Quantum computing applications: Simulation (chemistry) & Optimization

#### IBM: Towards Quantum Advantage in Financial Market Risk using Quantum Gradient Algorithms

#### 24 Nov 2021

New estimates for Quantum Advantage for computing Option Greeks – 6,000 qubits, 1MHz speed – 50 times lower than previous best estimates

https://arxiv.org/abs/2111.12509



#### Rigetti Computing: Synthetic weather radar using hybrid quantum-classical machine learning

Quantum kernels can, in principle, perform fundamentally more complex tasks than classical learning machines. The results establish synthetic weather radar as an effective heuristic benchmark for quantum computing capabilities and set the stage for detailed quantum advantage benchmarking on a highimpact operationally relevant problem



#### **BMW:** Quantum Computing Challenge winners

#### 9 Dec 2021

#### 30 Nov 2021

#### https://arxiv.org/abs/2111.15605





# Ongoing experiments on error correction: Superconducting circuits

Article

# Exponential suppression of bit or phase errors with cyclic error correction



#### **Realization of an Error-Correcting Surface Code with Superconducting Qubits**

Youwei Zhao,<sup>1,2,3,\*</sup> Yangsen Ye,<sup>1,2,3,\*</sup> He-Liang Huang,<sup>1,2,3,\*</sup> Yiming Zhang,<sup>1,2,3</sup> Dachao Wu,<sup>1,2,3</sup> Huijie Guan,<sup>1,2,3</sup> Qingling Zhu,<sup>1,2,3</sup> Zuolin Wei,<sup>1,2,3</sup> Tan He,<sup>1,2,3</sup> Sirui Cao,<sup>1,2,3</sup> Fusheng Chen,<sup>1,2,3</sup> Tung-Hsun Chung,<sup>1,2,3</sup> Hui Deng,<sup>1,2,3</sup> Daojin Fan,<sup>1,2,3</sup> Ming Gong,<sup>1,2,3</sup> Cheng Guo,<sup>1,2,3</sup> Shaojun Guo,<sup>1,2,3</sup> Lianchen Han,<sup>1,2,3</sup> Na Li,<sup>1,2,3</sup> Shaowei Li,<sup>1,2,3</sup> Yuan Li,<sup>1,2,3</sup> Futian Liang,<sup>1,2,3</sup> Jin Lin,<sup>1,2,3</sup> Haoran Qian,<sup>1,2,3</sup> Hao Rong,<sup>1,2,3</sup> Hong Su,<sup>1,2,3</sup> Lihua Sun,<sup>1,2,3</sup> Shiyu Wang,<sup>1,2,3</sup> Yulin Wu,<sup>1,2,3</sup> Yu Xu,<sup>1,2,3</sup> Chong Ying,<sup>1,2,3</sup> Jiale Yu,<sup>1,2,3</sup> Chen Zha,<sup>1,2,3</sup> Kaili Zhang,<sup>1,2,3</sup> Yong-Heng Huo,<sup>1,2,3</sup> Chao-Yang Lu,<sup>1,2,3</sup> Cheng-Zhi Peng,<sup>1,2,3</sup> Xiaobo Zhu,<sup>1,2,3</sup> and Jian-Wei Pan<sup>1,2,3</sup>

> <sup>1</sup>Department of Modern Physics, University of Science and Technology of China, Hefei 230026, China <sup>2</sup>Shanghai Branch, CAS Center for Excellence in Quantum Information and Quantum Physics, University of Science and Technology of China, Shanghai 201315, China <sup>3</sup>Shanghai Research Center for Quantum Sciences, Shanghai 201315, China



FIG. 1. Layout and circuit implementation. (a) Structure schematic of distance-three surface code. 17 qubits are choosen from *Zuchongzhi* 2.1 superconducting quantum processor, with 8 data qubits(gray dots), 4 Z-type ancilla qubits(green dots) and 4 X-type ancilla qubits(red dots). Each pair of qubits are connected with a coupler(black rectangle). Connecting lines are colored according

### Ongoing experiments on error correction: Rydberg atoms

#### A quantum processor based on coherent transport of entangled atom arrays

Dolev Bluvstein<sup>1</sup>, Harry Levine<sup>1,†</sup>, Giulia Semeghini<sup>1</sup>, Tout T. Wang<sup>1</sup>, Sepehr Ebadi<sup>1</sup>, Marcin Kalinowski<sup>1</sup>, Alexander Keesling<sup>1,2</sup>, Nishad Maskara<sup>1</sup>, Hannes Pichler<sup>3,4</sup>, Markus Greiner<sup>1</sup>, Vladan Vuletić<sup>5</sup>, and Mikhail D. Lukin<sup>1</sup>



FIG. 1. Quantum information architecture enabled by coherent transport of neutral atoms. a, In our approach, qubits are transported to perform entangling gates with distant qubits, enabling programmable and nonlocal connectivity. Atom shuttling is performed using optical tweezers, with high parallelism in two dimensions and between multiple zones allowing selective manipulations. Inset shows the atomic levels used: the  $|0\rangle$ ,  $|1\rangle$  qubit states refer to the  $m_F = 0$  clock states of <sup>87</sup>Rb, and  $|r\rangle$  is a Rydberg state used for generating entanglement between qubits (Extended Data Fig. 1b). b, Atom images illustrating coherent transport of entangled qubits. Using a sequence of single-qubit and two-qubit gates, atom pairs are each prepared in the  $|\Phi^+\rangle$  Bell state (Methods), and are then separated by 110  $\mu$ m over a span of 300  $\mu$ s. c, Parity oscillations indicate that movement does not observably affect entanglement or coherence. For both the moving and stationary measurements, qubit coherence is preserved using an XY8 dynamical decoupling sequence for 300  $\mu$ s (Methods). d, Measured Bell state fidelity as a function of separation speed over the 110  $\mu$ m, showing that fidelity is unaffected for a move slower than 200  $\mu$ s (average separation speed of 0.55  $\mu$ m/ $\mu$ s). Inset: normalizing by atom loss during the move results in constant fidelity, indicating that atom loss is the dominant error mechanism (see Methods for details).



# Ongoing experiments on error correction: lons

#### **Entangling logical qubits with lattice** surgery



Received: 23 September 2020





Fig. 1 | The Bacon-Shor subsystem code implemented on a 15-ion chain. Bacon-Shor is a [[9,1,3]] subsystem code that encodes nine data qubits into  $one \, logical \, qubit. \, Four \, weight-six \, stabilizers \, are \, mapped \, to \, ancillary \, qubits$ 

encoding of the logical qubit, with subsequent logical gate operations or error syndrome extraction.

#### Fast universal quantum gate above the fault-tolerance threshold in silicon

https://doi.org/10.1038/s41586-021-04182-y

Received: 4 August 2021

Accepted: 26 October 2021

#### **Precision tomography of a three-qubit** donor quantum processor in silicon

Giordano Scappucci<sup>3,5</sup> & Seigo Tarucha<sup>1,2</sup>

https://doi.org/10.1038/s41586-021-04292-7

Received: 29 June 2021

Accepted: 29 November 2021

Published online: 19 January 2022

Mateusz T. Mądzik<sup>1,9,12</sup>, Serwan Asaad<sup>1,10,12</sup>, Akram Youssry<sup>2,3</sup>, Benjamin Joecker<sup>1</sup>, Kenneth M. Rudinger<sup>4</sup>, Erik Nielsen<sup>4</sup>, Kevin C. Young<sup>5</sup>, Timothy J. Proctor<sup>5</sup>, Andrew D. Baczewski<sup>6</sup>, Arne Laucht<sup>1,2</sup>, Vivien Schmitt<sup>1,11</sup>, Fay E. Hudson<sup>1</sup>, Kohei M. Itoh<sup>7</sup>, Alexander M. Jakob<sup>8</sup>, Brett C. Johnson<sup>8</sup>, David N. Jamieson<sup>8</sup>, Andrew S. Dzurak<sup>1</sup>, Christopher Ferrie<sup>2</sup>, Robin Blume-Kohout<sup>4</sup> & Andrea Morello<sup>1</sup><sup>∞</sup>

Akito Noiri<sup>1</sup>, Kenta Takeda<sup>1</sup>, Takashi Nakajima<sup>1</sup>, Takashi Kobayashi<sup>2</sup>, Amir Sammak<sup>3,4</sup>,

#### Quantum logic with spin qubits crossing the surface code threshold

https://doi.org/10.1038/s41586-021-04273-w

Xiao Xue<sup>1,2</sup>, Maximilian Russ<sup>1,2</sup>, Nodar Samkharadze<sup>1,3</sup>, Brennan Undseth<sup>1,2</sup>, Amir Sammak<sup>1,3</sup>, Giordano Scappucci<sup>1,2</sup> & Lieven M. K. Vandersypen<sup>1,2</sup>

Received: 1 July 2021

Semiconductor qubits below the error threshold

#### 2-qubit gate fidelity of 99.5

2-qubit average gate fidelity of 99.37(11)% and two-qubit preparation/measurement fidelities of 98.95(4)%

1-qubit and 2-qubit gate fidelities, all of which are above 99.5%, extracted from gate-set tomography

# Towards practical applications: Quantum annealing (for optimization and machine learning) and quantum chemistry

A.S. Boev, et. al. Genome assembly using quantum and quantum-inspired annealing, Scientific Reports 11, 13183 (2021); arXiv:2004.06719;

A. Gircha, et. al., Training a discrete variational autoencoder for generative chemistry and drug design on a quantum annealer, arXiv:2108.11644.

M. Sapova and A.K. Fedorov, Variational quantum eigensolver techniques for simulating carbon monoxide oxidation, arXiv:2108.11167

# From universal quantum computers to special-purpose quantum devices

#### D-Wave quantum annealer for QUBO problems



Lack of connectivity, coherence, violating adiabatic evolution, access for experiments

#### Rydberg programmable quantum simulators for MIS problems







Potentially better coherence, connectivity, not yet widely available

#### From universal quantum computers to special-purpose quantum devices

It consists in finding the bit string  $(\sigma_i = \pm 1)$  that minimize the objective function,  $H = \sum_i R_i \sigma_i - \frac{1}{2} \sum_{i,j} J_{ij} \sigma_i \sigma_j$ , where  $R_i$  is the "bias vector" and  $J_{ij} = J_{ji}$  is a given "coupling matrix". This objective function emerges in solid state physics under the name of Ising models, hence QUBO is sometimes referred to as Ising problem.

Many potential applications:

- designing metamaterials,
- quantum chemistry (not scalable),
- protein folding (not scalable),
- financial portfolio optimization,
- forecasting financial crashes,
- scheduling





#### Quantum annealing for a genome assembly problem





Figure 1. Solving the *de novo* genome assembly problem using quantum annealers and quantum-inspired (digital) annealing algorithms: (a) raw reads; (b) raw reads are transformed to the overlap-layout-consensus (OLC) graph; (c) finding the Hamiltonian path for the OLC graph is reduced to the QUBO problem; (d) the QUBO problem should be embedded to the architecture of the quantum annealer (D-Wave): for this purpose each logical variable of the the QUBO problem is assigned with several qubits of the quantum annealer; (e) and (f) the Ising problem in QUBO form can be solved using quantum annealers (D-Wave) and quantum-inspired algorithms (SimCIM), correspondingly; (g) the output is the Hamiltonian path; (h) the genome sequence is obtained as the solution.

# Quantum annealing for a genome assembly problem

		Mean, µs	Min, µs	Max, µs	90%
O	CPU	8483	8314	8619	8579
Quantum annealer	QPU	535	369	672	600
Quantum-inspired annealer (SimCIM)		262	9.9	7212	1061

**Table 1.** Genome assembly time for  $\phi X$  174 bacteriophage for 1000 instances. For the data based on experiments with quantum annealers we highlight required classical processor unit (CPU) time and quantum processor unit (QPU) time.

#### Experiments characteristics:

- annealing time = 20 microseconds;
- annealing runs =  $10^3$ ;
- standard configurations of the processor.

### Quantum annealing for a genome assembly problem

Sequence length	Graph size	Qubo size	Physical qubits	
5	3	9	36	
6	4	16	80	
7	5	25	200	
8	6	36	360	
9	7	49	686	
10	8	64	1088	





of physical qubits and other limitations... need better hardware (coherence and connectivity)

#### $TTS = t_a R_{99}$ ,

Figure 2. Comparison of the performance of quantum and quantum-inspired methods for *de novo* genome assembly based on synthetic data (10 problems were generated for every sequence length): we compare TTS for quantum device D-Wave and quantum-inspired optimization algorithm SimCIM.

# Competitive behaviour for small-size data, but growing overhead in the size of the problem number





# Quantum annealing for generative chemistry



Fig. 3 The autoencoder and the variational autoencoder. a An autoencoder encodes input molecules into compressed representations and decodes them back. b A variational autoencoder maps the

- space is a continuous numerical representation

#### Quantum annealing for training

Existing special-purpose quantum devices can be used for this purpose. Dumoulin et al. [325] and Benedetti et al. [326] pointed out that quantum annealers that have strong interaction with the environment freeze out the dynamics of a spin system before the termination of the annealing process. As a result, such annealers sample from a thermal distribution with some finite temperature. The proposed method was experimentally implemented using the D-Wave 2X quantum annealer [97, 326] for the training of a Boltzmann machine. However, shortcomings of existing quantum annealers (see Box 8) limited the study to low-dimensional datasets.



#### **Training Restricted Boltzmann Machines With a D-Wave Quantum** Annealer

Vivek Dixit<sup>1,2</sup>, Raja Selvarajan<sup>1,2</sup>, Muhammad A. Alam<sup>3,4</sup>, Travis S. Humble<sup>5</sup> and Sabre Kais 1,2,4\*

<sup>1</sup>Department of Chemistry, Purdue University, West Lafayette, IN, United States, <sup>2</sup>Department of Physics and Astronomy, Purdue University, West Lafayette, IN, United States, <sup>3</sup>Department of Electrical and Computer Engineering, Purdue University, West Lafayette, IN, United States, <sup>4</sup>Birck Nanotechnology Center, Purdue University, West Lafayette, IN, United States, <sup>5</sup>Quantum Computing Institute, Oak Ridge National Laboratory, Oak Ridge, TN, United States

Restricted Boltzmann Machine (RBM) is an energy-based, undirected graphical model. It is commonly used for unsupervised and supervised machine learning. Typically, RBM is trained using contrastive divergence (CD). However, training with CD is slow and does not estimate the exact gradient of the log-likelihood cost function. In this work, the model expectation of gradient learning for RBM has been calculated using a quantum annealer (D-Wave 2000Q), where obtaining samples is faster than Markov chain Monte Carlo (MCMC) used in CD. Training and classification results of RBM trained using quantum annealing are compared with the CD-based method. The performance of the two approaches is compared with respect to the classification accuracies, image reconstruction, and log-likelihood results. The classification accuracy results indicate comparable performances of the two methods. Image reconstruction and loglikelihood results show improved performance of the CD-based method. It is shown that the samples obtained from quantum annealer can be used to train an RBM on a 64-bit "bars and stripes" dataset with classification performance similar to an RBM trained with CD. Though training based on CD showed improved learning performance, training using a quantum annealer could be useful as it eliminates computationally expensive MCMC steps of CD.





# Quantum annealing for generative chemistry



The model learns useful representations of chemical structures from ChEMBL, which is the manually curated database of biologically active molecules with drug-like properties



Figure 1. Scheme of the DVAE learning a joint probability distribution over the molecular structural features x and their latent variable-representations (discrete z and continuous  $\zeta$ ). Here,  $q_{\phi}(z|x)$  and  $p_{\theta}(x|\zeta)$  are the encoder and decoder distributions, respectively, whereas  $p_{\theta}(z)$  is the prior distribution in the latent variable space and is approximated by RBM. We provide an example of reconstruction of a target molecule (diaveridine) using Gibbs-300 model saved after 300 epochs of training (here t is the Tanimoto similarity between the initial molecule and its reconstruction, t = 1.0 corresponds to perfect reconstruction, p is the output probability).

The two layers of RBM contain 128 units each since an RBM of precisely this size could be sampled on readily available quantum annealers.



Figure 2. Learning curves of DVAE trained with classical Gibbs sampleing (red) and samples from D-Wave annealer (blue). Training on D-Wave suspended before reaching convergence due to resource limitation.

# Quantum annealing for generative chemistry

	Train set	D-Wave sampl.	Gibbs sampl.	Gibbs sa
		(75 epochs)	(75 epochs)	(300 epc
MW	409.99	374.16	397.81	416.1
LogP	3.41	3.68	3.64	3.61
QED	0.54	0.54	0.54	0.52
SAS	2.96	3.12	3.04	3.13
Validity	1.0	0.54	0.55	0.69

Table I. The parameters of distributions of basic physical and medicinal chemistry properties of the molecules produced by the generative models discussed in this work. The entries in the table are mean values computed with the help of RDKit library [29] to obtain the molecular weight (MW), LogP, QED, and the synthetic accessibility score (SAS) [28].

We kept track of molecular weight (MW), the water-octanol partition coefficient (logP), the synthetic accessibility, and drug-likeness (QED) scores; we generated 2331 novel chemical structures with medicinal chemistry and synthetic accessibility properties in the ranges typical for molecules from ChEMBL.





Figure 3. Distributions of basic physical and medicinal chemistry properties of the molecules produced by the proposed generative models discussed (same as in Table I).



# Variational quantum algorithms



Figure 2 Diagrammatic representation of a Variational Quantum Algorithm (VQA). A VQA workflow can be divided into four main components: i) the objective function O that encodes the problem to be solved; ii) the parameterized quantum circuit (PQC), in which its parameters  $\theta$  are tuned to minimize the objective; *iii*) the measurement scheme, which performs the basis changes and measurements needed to compute expectation values  $\langle H \rangle$  that are used to evaluate the objective; and iv) the classical optimizer that minimizes the objective and proposes a new set of variational parameters. The PQC can be defined heuristically, following hardware-inspired ansätze, or designed from the knowledge about the problem Hamiltonian H. It can also include a state preparation unitary  $P(\phi)$  which situates the algorithm to start in a particular region of parameter space. Inputs of a VQA are the circuit ansatz  $\mathcal{U}(\theta, \phi)$  and the initial parameter values  $\theta_0, \phi_0$ . Outputs include optimized parameter values  $\theta_{\text{opt}}, \phi_{\text{opt}}$  and the minimum of the objective.





# Variational quantum algorithms: VQE

#### Variational Quantum Eigensolver (VQE) is a flagship hybrid quantum-classical algorithm for molecular simulations. An extended family of algorithms.

where  $|\psi\rangle$  is the ansatz at the current iteration to be ADAPT-VQE. Early variational algorithms employed a updated. After computing the gradient components and fixed ansatz design, with its parameters tuned using choosing the operator corresponding to the largest grasome classical optimizer. The "Adaptive Derivativedient, the gate operation implementing  $\hat{\tau}_i$  is added to Assembled Pseudo-Trotter ansatz Variational Quantum the ansatz with its parameter value initialized at 0. The Eigensolver" (ADAPT-VQE) was introduced as a more ansatz is then optimized before growing another operascalable and efficient way to simultaneously design and tor. The ADAPT-VQE algorithm terminates when the optimize a parameterized ansatz (Grimsley et al., 2019b). norm of the gradient vector falls below a defined thresh-At each iteration, ADAPT-VQE constructs an ansatz by old. In the case of fermionic ADAPT-VQE, the operator adding an operator corresponding to the largest gradient pool consists of fermionic operators that are transformed from a carefully designed operator pool. That is, given into quantum gate operations through e.g. the Jordanan operator  $\hat{\tau}_i$  from the operator pool, the gradient of the Wigner mapping. A more "hardware-efficient" variant of energy with respect to the corresponding parameter  $\theta_i$  is the ADAPT-VQE algorithm is the qubit ADAPT-VQE, defined as in which the pool consists of gate operators acting directly on qubits (Tang et al., 2019). Both versions of 9) ADAPT-VQEs were able to to generate optimized circuits with reduced depths and CNOT counts compared to previous ansatz construction and optimization methods.

$$\partial_i E = \langle \psi | [H, \hat{\tau}_i] | \psi \rangle, \qquad (49)$$

# Variational quantum algorithms: VQE



Figure 1. Scheme of the ansatz growing procedure in original and batched ADAPT-VQE. At each iteration, the original ADAPT-VQE adds a single operator with the largest gradient value. In our implementation of batched ADAPT-VQE, at each step of the ansatz growing procedure we add multiple operators with largest gradients; k is the number of gradients that differ from the largest one by less than r.



# First results of VQE for O<sub>2</sub>, CO, CO<sub>2</sub>: 20-qubit emulator



ADAPT-VQE convergence.

Figure 3. Energy convergence for the considered implementations of ADAPT-VQE and VQE-UCCSD methods for O<sub>2</sub> (a), CO (b) and CO<sub>2</sub> (c) molecules. We run batched ADAPT-VQE for all molecules beyond the simulation of original ADAPT-VQE. While for  $O_2$  and CO molecules the original implementation converges, batched implementation continues to improve the energy. For  $CO_2$ , the original ADAPT-VQE takes infeasible amount of time, while batched version is much faster. We run limited iterations of the original ADAPT-VQE implementation to verify the similarity with batched





# Error correction codes: First steps

### Error correction codes: First ideas and tests

- Wide class of codes (Special structure of stabilisers): repetition codes, Shor's code,...
- Circle-like connectivity (no all-to-all / ancillato-all)
- Low-noise two-qubit gates
- New efficient decoding system





#### <u>3-qubit code</u>





## Characterizing noisy devices

### NISQ devices as open quantum systems

Challenge: analyze and predict dynamics of open quantum systems





- FIG. 2. A crystal of 38 laser-cooled <sup>24</sup>Mg<sup>+</sup> ions loaded with the LED-loading method. Fluorescence from laser radiation at 280 nm is recorded by an EMCCD camera. Dark sites correspond to ions of other isotopes or elements.
  - I. Zalivako et. al., Appl. Phys. Lett. 115, 104102 (2019)





### NISQ devices as open quantum systems: Learning

Goal is to analyze non-equilibrium dynamical effects of quantum physics. One of the problems is to make a prediction of the dynamics.



Markovian dynamics).





- A possible solution: to use a data-driven approach (learning non-
- <u>Advantages</u>: can be based on experimentally observed data.
- Disadvantages: "black-box" approaches (no physical insights about the system), scalability, convergence, and model selection.



a) Extraction of quantum trajectories via quantum tomography of system states at discrete time moments. b) Main building blocks of the input data processing and connections between blocks. c) Dynamics prediction based on the reconstructed Markovian embedding.

# Dynamics prediction and denoising for various models







# Characterizing quantum channels (processes)





Figure 3. In (a) distribution of fidelity confidence intervals as the function of (one minus) CL over 100 numerical experiments for depolarizing channel and different values of n is shown. The single confidence interval for  $n = 10^3$  is highlighted. The dashed line shows the true value of the fidelity. In (b) the circuit of the QPT protocol for the quantum teleportation channel is depicted (standard notations for Hadamard gate, controlled-NOT gate, and computational basis readout measurement are used). Gates U and V consistently take forms shown in the right-hand side, where  $R_{x(y)}^{\bullet}$  is the standard rotation around x(y) axis of the Bloch sphere (12 configurations of the circuit is run in total). The imperfections of readout computational basis measurement are also taken into account. In (c) the resulting fidelity confidence intervals for the QPT experiment from (b) run on IBM quantum experience superconducting processor is demonstrated. The dash line shows fidelity of the reconstructed point estimate of the

### Alternative quantum computing platforms

### Progress in developing qudit-based processors



#### A universal qudit quantum processor with trapped ions

Martin Ringbauer,<sup>1</sup> Michael Meth,<sup>1</sup> Lukas Postler,<sup>1</sup> Roman Stricker,<sup>1</sup> Rainer Blatt,<sup>1,2,3</sup> Philipp Schindler,<sup>1</sup> and Thomas Monz<sup>1,3</sup>

<sup>1</sup>Institut für Experimentalphysik, Universität Innsbruck, Technikerstrasse 25, 6020 Innsbruck, Austria <sup>2</sup>Institut für Quantenoptik und Quanteninformation,

Österreichische Akademie der Wissenschaften, Otto-Hittmair-Platz 1, 6020 Innsbruck, Austria <sup>3</sup>Alpine Quantum Technologies GmbH, 6020 Innsbruck, Austria

Today's quantum computers operate with a binary encoding that is the quantum analog of classical bits. Yet, the underlying quantum hardware consists of information carriers that are not necessarily binary, but typically exhibit a rich multilevel structure, which is artificially restricted to two dimensions. A wide range of applications from quantum chemistry to quantum simulation, on the other hand, would benefit from access to higher-dimensional Hilbert spaces, which conventional quantum computers can only emulate. Here we demonstrate a universal qudit quantum processor using trapped ions with a local Hilbert space dimension of up to 7. With a performance similar to qubit quantum processors, this approach enables native simulation of high-dimensional quantum systems, as well as more efficient implementation of qubit-based algorithms.

#### d=7 Trapped ions

# rigetti

# Beyond Qubits: Unlocking the Third State in Quantum

#### Processors





By Alex Hill, Senior Quantum Systems Engineer

#### d=3 Superconducting circuits

### Results of 2020-2021: Qudit-based processor @ Lebedev Institute and RQC





### **Qudit-based compiler**

#### Running qubit circuit with qudit-based processor (emulator)



1) Maximizing the total fidelity:

2) Brute-force search for small-scale circuits;

3) Approximate search for more complicated sit (finding not the optimal, but better decomposition)

A.S. Nikolaeva, E.O. Kiktenko, and A.K. Fedorov, https://arxiv.org/abs/2113.04384

$$\mathcal{F}(\phi) = \prod_{i=1}^{D(\phi)} \left( 1 - e_{\text{est}}(U_i^{\text{qd}}(\phi)) \right),$$

# Qudit-based compiler: Example

![](_page_39_Figure_1.jpeg)

Figure 3. (a) Example of the input hardware-agnostic qubit circuit on n = 5 qubits (standard notations for CNOT, Hadamard gate, generalized Toffoli gate, and computational basis measurements are used). (b) Qubit-to-qudit mapping that is used for the realization of the given qubit circuit with m = 4 qudits and d = 4 levels. (c) Equivalence of read-out results that are obtained with qudit-based emulator and post-processed outputs, which can be interpreted as results of the circuit implementation. (d) Qubit-based transpilation for the input qubit circuit down to single-qubit gates and Toffoli gates. (e) Qubit-based transpilation for the Toffoli gate down to CNOT and single-qubit gates. (f) Qubit-based transpilation for the input qubit circuit down to the basic single-qudit and two-qudit generalized controlled gates (see Fig. 2a for the possibilities of the further transpilation).

Qubit-based decomposition: <u>31 two-qubit</u> <u>gates</u>.

Qudit-based decomposition: **5 two-qudit** gates.

# Results of 2020-2021: LRC

![](_page_40_Picture_1.jpeg)

![](_page_40_Figure_2.jpeg)

https://lrc-quantum.ru/login

# Thank you for your attention!

![](_page_41_Picture_1.jpeg)

#### Invitation to publish in EPJ QT

![](_page_41_Picture_3.jpeg)

![](_page_42_Figure_0.jpeg)

are discussed and shown to be erroneous.

![](_page_42_Figure_5.jpeg)

#### Error correction codes: Shor's code

#### Structure for the Shor's code

![](_page_43_Figure_2.jpeg)

![](_page_43_Figure_3.jpeg)

### Probing non-Markovian dynamics

![](_page_45_Figure_1.jpeg)

*K* is usually set knowingly large in order to capture all memory effects

**r** allows revealing an effective number of unknown degrees of freedoms, which are necessary to be taken into account in order to predict the state of the system; "Measure" of non-Markovianity and complexity of simulating dynamics of an open quantum systems

![](_page_45_Figure_6.jpeg)

Reconstructed Markovian embedding can be used for predicting the non-Markovian dynamics of the system, given a sequence of states at the first K time steps

![](_page_46_Figure_2.jpeg)

 $\varrho(K+n-1) = \mathbf{D}\left[\Lambda_r^n \mathbf{E}[\varrho(K-1), \varrho(K-2), \dots, \varrho(0)]\right].$ 

$$\stackrel{s(K-1+n)}{\longrightarrow} \overbrace{\mathcal{O}(K-1+n)}^{}$$

![](_page_47_Figure_1.jpeg)

 $(\varrho(0), \varrho(1), \ldots)$  system's trajectories: Input data for our analysis

arrho(k+1) depends on the whole prehistory

Quantum trajectories are irregular and challenging for further analysis even in the case of low-dimensional systems

![](_page_47_Picture_5.jpeg)

$$(\varrho(k), \varrho(k-1), \ldots)$$

![](_page_48_Figure_1.jpeg)

K is usually set knowingly large in order to capture all memory effects

**r** allows revealing <u>an effective number of unknown degrees</u> of freedoms, which are necessary to be taken into account in order to predict the state of the system.

The concept of the effective dimension of the environment: the minimal possible dimension of the environment that reproduces the same non-Markovian dynamics of the system:

 $d_{\rm E}^{\rm eff} = \left|\sqrt{r/d^2}\right|$ 

"Measure" of non-Markovianity and complexity of simulating dynamics of an open quantum systems

Dimensionality of the system

![](_page_48_Figure_8.jpeg)

![](_page_48_Picture_9.jpeg)

#### Details of the approach: Nakajima-Zwanzig equation and Markovian embedding

Discrete time version of the Nakajima-Zwanzig equation:

$$\varrho(k+1) = \sum_{i=1}^{K} \mathcal{M}_i[\varrho(k-K+i)], \quad k \in \{K-1, K, \ldots\},$$

Vectorized form:

$$|\varrho(k+1)\rangle = M \begin{bmatrix} |\varrho(k-K+1)\rangle \\ \vdots \\ |\varrho(k)\rangle \end{bmatrix}, \quad M := \begin{bmatrix} M_1 & \dots & M_K \end{bmatrix}, \quad \exists |i\rangle \langle j| \mapsto |i\rangle \otimes |j\rangle$$

Nakajima-Zwanzig equation and a Markovian embedding:

$$R(k+1) = \overline{M}R(k), \quad R(k) := egin{bmatrix} ert arrho(k-K+1) 
angle \ ert arrho \ ert arrho \ ert arrho(k) 
angle \end{bmatrix} \qquad \overline{M} := egin{bmatrix} 0 & \ldots & 0 & ert \ ert arrho & ert arrho \ ert arrho arrho arrho arrho \ ert arrho arrho arrho arrho arrho \ ert arrho(k) 
angle \end{bmatrix},$$

Reinforcement learning: Partially observed environment

50

![](_page_49_Picture_10.jpeg)

### Details of the approach: Nakajima-Zwanzig equation and Markovian embedding

Nakajima

-Zwanzig equation and a Markovian embedding:  

$$R(k+1) = \overline{M}R(k), \quad R(k) := \begin{bmatrix} |\varrho(k-K+1)\rangle\rangle \\ \vdots \\ |\varrho(k)\rangle\rangle \end{bmatrix} \qquad \overline{M} := \begin{bmatrix} d^{2}(K-1) \times d^{2} & (K-1)d^{2} \times (K-1)d^{2} \\ 0 & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & 0 & 0 & \dots & 1 \\ \hline M \end{bmatrix},$$

if we consider R(k) as the state of some new abstract system at a discrete time moment k, then the next state R(k+1) depends only on R(k) and the time-independent dynamics generator M. All these states belong to some rdimensional subspace R, where r can be less than Kd<sup>2</sup>. This fact can be used to reduce the dimension.

$$R(k+1) = \overline{M}R(k) \longrightarrow R(k+1) = \overline{M}\pi_{\mathcal{R}}R(k),$$

Eigendecomposition:

$$\overline{M}\pi_{\mathcal{R}} = Q^{-1}\Lambda Q,$$

only r leading eigenvalues from  $\Lambda$  are non-zero.

Truncation:

$$D := Q^{-1}[:,:r], \quad E := Q[:r,:], \quad \Lambda_r := \Lambda[:r,:r],$$

where  $\pi_{\mathcal{R}}$  is the orthogonal projection matrix on the subspace  $\mathcal{R}$ Physical trajectories

![](_page_50_Figure_11.jpeg)

![](_page_50_Picture_13.jpeg)

![](_page_50_Picture_14.jpeg)

#### Details of the approach

The truncated eigendecomposition allows compressing R(k)

Alternatively:

![](_page_51_Figure_3.jpeg)

![](_page_51_Figure_4.jpeg)

 $R(k+n) = D\Lambda_r^n E R(k),$ 

Embedding evolution  $s(k+1) = \Lambda_r s(k).$ 

$$\Lambda_r^n \xrightarrow{s(K-1+n)} D \rightarrow \varrho(K-1+n)$$

#### **Initial data:**

$$S_{\text{noisy}} = \{\mathcal{T}_{\text{noisv}}^{(1)}, \mathcal{T}_{\text{noisv}}^{(2)}, \dots, \mathcal{T}_{\text{noisv}}^{(L)}\}$$
$$\mathcal{T}_{\text{noisy}}^{(i)} = \left(\varrho_{\text{noisy}}^{(i)}(0), \varrho_{\text{noisy}}^{(i)}(1), \dots, \varrho_{\text{noisy}}^{(i)}(T-1)\right)$$
Memory depth hyper-parameter (K)  
Noise std

#### Output:

the minimal Markovian embedding dimension (r)

![](_page_52_Picture_5.jpeg)

 $D, E, \Lambda_r$  (dynamics)

+

**Denoised trajectories** 

#### We construct three auxiliary matrices:

$$H_{\text{noisy}}^{(i)} = \begin{bmatrix} |\varrho_{\text{noisy}}^{(i)}(0)\rangle & |\varrho_{\text{noisy}}^{(i)}(1)\rangle & \dots & |\varrho_{\text{noisy}}^{(i)}(1)\rangle \\ |\varrho_{\text{noisy}}^{(i)}(1)\rangle & |\varrho_{\text{noisy}}^{(i)}(2)\rangle & \dots & |\varrho_{\text{noisy}}^{(i)}(1)\rangle \\ \vdots & \vdots & \ddots \\ |\varrho_{\text{noisy}}^{(i)}(K-1)\rangle & |\varrho_{\text{noisy}}^{(i)}(K)\rangle & \dots & |\varrho_{\text{noisy}}^{(i)}(1)\rangle \\ X_{\text{noisy}}^{(i)} = H_{\text{noisy}}^{(i)}[:,:-1], \quad Y_{\text{noisy}}^{(i)} = H_{\text{noisy}}^{(i)}[:,1:], \end{bmatrix}$$

X and Y are shifted one step relative to each other

Then we stack matrices within sets of multiple trajectories:

$$\begin{aligned} X_{\text{noisy}} &= \begin{bmatrix} X_{\text{noisy}}^{(1)} & X_{\text{noisy}}^{(2)} & \dots & X_{\text{noisy}}^{(L)} \\ Y_{\text{noisy}} &= \begin{bmatrix} Y_{\text{noisy}}^{(1)} & Y_{\text{noisy}}^{(2)} & \dots & Y_{\text{noisy}}^{(L)} \\ H_{\text{noisy}} &= \begin{bmatrix} H_{\text{noisy}}^{(1)} & H_{\text{noisy}}^{(2)} & \dots & H_{\text{noisy}}^{(L)} \\ \end{bmatrix} \end{aligned}$$

,  $_{\text{noisy}}^{(i)}(T)\rangle\rangle$ 

![](_page_53_Picture_7.jpeg)

![](_page_53_Figure_9.jpeg)

![](_page_53_Picture_10.jpeg)

![](_page_53_Figure_12.jpeg)

We introduce a low-rank approximation and then recast it back into the set of trajectories. The optimal approximation of H\_noisy can be obtained using singular value decomposition (SVD):

$$H_{\eta} = U[:,:\eta]S[:\eta,:\eta]V[:,:\eta]^{\dagger},$$

The optimal rank than leads to the best denoising of a matrix without significant states distortion can be estimated by using the method of Gavish and Donoho (2014):

$$\begin{split} \eta_{\text{opt}} &= \sum_{i} \text{trunc}_{\sigma}(S[i,i]), \\ \text{trunc}_{\sigma}(x) &= \begin{cases} 1, & x \geq \sigma \sqrt{2}\sqrt{n}f\left(\frac{m}{n}\right), \\ 0, & \text{otherwise}, \end{cases} \\ f(\beta) &= \sqrt{2(\beta+1) + \frac{8\beta}{(\beta+1) + \sqrt{\beta^2 + 14\beta + \beta^2}}} \end{split}$$

$$H_{\text{denoised}} = H_{\eta_{\text{opt}}}.$$

$$r = \eta_{\text{opt}}.$$

#### **Denoised versions:**

 $X_{\text{denoised}} = U[:,:\eta_{\text{opt}}]U[:,:\eta_{\text{opt}}]^{\dagger}X_{\text{noisy}},$  $Y_{\text{denoised}} = U[:,:\eta_{\text{opt}}]U[:,:\eta_{\text{opt}}]^{\dagger}Y_{\text{noisy}}.$ 

Minimization wrt to Frobenius norm:

$$\overline{M} = \underset{W}{\operatorname{argmin}} \|Y_{\text{denoised}} - WX_{\text{denoised}}\|_{\mathrm{F}},$$

Reconstructing encoding and decoding matrices from M:

$$\overline{M}\pi_{\mathcal{R}} = Q^{-1}\Lambda Q, \qquad \qquad D:$$

![](_page_55_Figure_7.jpeg)

**Optimal-rank solution:** 

$$\overline{M}_{\eta_{\rm opt}} = Y_{\rm denoised} X_{\rm denoised}^+,$$

 $x = Q^{-1}[:,:r], \quad E := Q[:r,:], \quad \Lambda_r := \Lambda[:r,:r],$ 

#### **Dynamics prediction is possible!**

# Predicted Markovian embedding minimal dimension

Qubit with a finite dimensional environment; we sample at random a quantum dynamical semigroup generator in the GKSL form. We simulate noise appearing during data acquisition of trajectories.

![](_page_56_Figure_2.jpeg)

The method works correctly and predicts the irregular non-Markovian dynamics of a qubit

![](_page_56_Picture_5.jpeg)

### Selection of the memory depth hyperparemeter

Qubit with a finite dimensional environment; we sample at random a quantum dynamical semigroup generator in the GKSL form. We simulate noise appearing during data acquisition of trajectories.

$$\mathcal{D}^{\text{test}}(\mathcal{T}_1, \mathcal{T}_2) = \frac{1}{T - K} \sum_{k=K}^{T-1} \|\varrho_1(k) - \varrho_2(k)\|_1,$$

![](_page_57_Figure_3.jpeg)

**'Saturation' value of K: starting from** which the accuracy of prediction is mainly determined by the noise level

![](_page_57_Picture_6.jpeg)

# Quality of deniosing

Qubit with a finite dimensional environment; we sample at random a quantum dynamical semigroup generator in the GKSL form. We simulate noise appearing during data acquisition of trajectories.

1,

![](_page_58_Picture_4.jpeg)

As a valuable by-product of the rank estimation we obtain the denoised version of a data set.

![](_page_58_Picture_7.jpeg)

# Reconstructing eigenfrequencies of the joint system

Qubit with a finite dimensional environment; we sample at random a quantum dynamical semigroup generator in the GKSL form. We simulate noise appearing during data acquisition of trajectories. A comparison of the spectrum of the quantum channel  $exp(\tau L)$  driving the dynamics of the joint system and environment density matrix with the diagonal elements of  $\Lambda_{c}$ 

![](_page_59_Figure_2.jpeg)

A perfect coincidence in the case without noise; in the presence of noise, we see that the approach provides valuable information about eigenfrequencies.

![](_page_59_Picture_5.jpeg)